KEY STAGE 2

In upper Key Stage 2, children build on secure foundations in calculation, and develop fluency, accuracy and flexibility in their approach to the four operations. They work with whole numbers and adapt their skills to work with decimals, and they continue to develop their ability to select appropriate, accurate and efficient operations.

Key language: decimal, column methods, exchange, partition, mental method, ten thousand, hundred thousand, million, factor, multiple, prime number, square number, cube number

Addition and subtraction: Children build on their column methods to add and subtract numbers with up to seven digits, and they adapt the methods to calculate efficiently and effectively with decimals, ensuring understanding of place value at every stage.

Children compare and contrast methods, and they select mental methods or jottings where appropriate and where these are more likely to be efficient or accurate when compared with formal column methods.

Bar models are used to represent the calculations required to solve problems and may indicate where efficient methods can be chosen.

Multiplication and division: Building on their understanding, children develop methods to multiply up to 4-digit numbers by single-digit and 2-digit numbers.

Children develop column methods with an understanding of place value, and they continue to use the key skill of unitising to multiply and divide by 10, 100 and 1,000.

Written division methods are introduced and adapted for division by single-digit and 2-digit numbers and are understood alongside the area model and place value. In Year 6, children develop a secure understanding of how division is related to fractions.

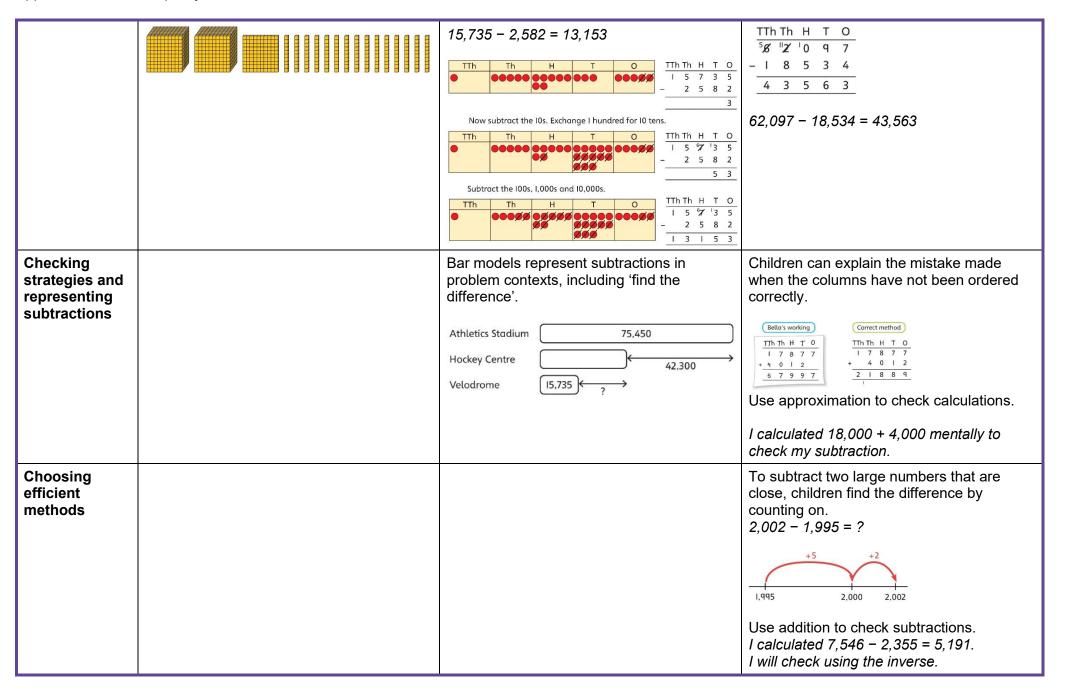
Multiplication and division of decimals are also introduced and refined in Year 6.

Fractions: Children find fractions of amounts, multiply a fraction by a whole number and by another fraction, divide a fraction by a whole number, and add and subtract fractions with different denominators. Children become more confident working with improper fractions and mixed numbers and can calculate with them. Understanding of decimals with up to 3 decimal places is built through place value and as fractions, and children calculate with decimals in the context of measure as well as in pure arithmetic.

Children develop an understanding of percentages in relation to hundredths, and they understand how to work with common percentages: 50%, 25%, 10% and 1%.

		Year 5	
	Concrete	Pictorial	Abstract
Year 5 Addition			
Column addition with whole numbers	Use place value equipment to represent additions. Add a row of counters onto the place value grid to show 15,735 + 4,012.	Represent additions, using place value equipment on a place value grid alongside written methods. TTh Th H T O 2 0 1 5 3 + 1 9 1 7 5 3 9 3 2 8	Use column addition, including exchanges. TTh Th
Representing additions		Bar models represent addition of two or more numbers in the context of problem solving. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Use approximation to check whether answers are reasonable. TTh Th
Adding tenths	Link measure with addition of decimals. Two lengths of fencing are 0.6 m and 0.2 m. How long are they when added together?	Use a bar model with a number line to add tenths.	Understand the link with adding fractions. $\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$

	0·6 m 0·2 m	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	6 tenths + 2 tenths = 8 tenths 0·6 + 0·2 = 0·8
Adding decimals using column addition	Use place value equipment to represent additions. Show 0·23 + 0·45 using place value counters.	Use place value equipment on a place value grid to represent additions. Represent exchange where necessary. O Tth Hth O Q Q 2 + O 3 3 I 2 5 Include examples where the numbers of decimal places are different. O Tth Hth O Q 2 + O 3 3 I 2 5 Include examples where the numbers of decimal places are different.	Add using a column method, ensuring that children understand the link with place value. $ \frac{O \cdot \text{Tth Hth}}{0 \cdot 2 \cdot 3} + \frac{0 \cdot 4 \cdot 5}{0 \cdot 6 \cdot 8} $ Include exchange where required, alongside an understanding of place value. $ \frac{O \cdot \text{Tth Hth}}{0 \cdot 9 \cdot 2} + \frac{0 \cdot 3 \cdot 3}{1 \cdot 2 \cdot 5} $ Include additions where the numbers of decimal places are different. $ 3.4 + 0.65 = ? $ $ \frac{O \cdot \text{Tth Hth}}{3 \cdot 4 \cdot 0} + \frac{0 \cdot 6 \cdot 5}{3 \cdot 2} $
Year 5 Subtraction			
Column subtraction with whole numbers	Use place value equipment to understand where exchanges are required. 2,250 – 1,070	Represent the stages of the calculation using place value equipment on a grid alongside the calculation, including exchanges where required.	Use column subtraction methods with exchange where required.

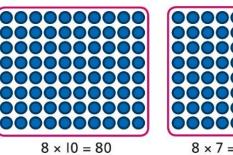


Subtracting decimals	Explore complements to a whole number by working in the context of length. $ \begin{array}{cccccccccccccccccccccccccccccccccc$	Use a place value grid to represent the stages of column subtraction, including exchanges where required. $5.74 - 2.25 = ?$ Sexchange I tenth for I0 hundredths. O Tth Hth $5.57.4$ - $2.2.55$ - $2.2.5$ Exchange I tenth for I0 hundredths. Now subtract the 5 hundredths. O Tth Hth $5.57.14$ - $2.2.55$ -
Year 5 Multiplication		
Understanding factors	Use cubes or counters to explore the meaning of 'square numbers'. 25 is a square number because it is made from 5 rows of 5. Use cubes to explore cube numbers.	Use images to explore examples and nonexamples of square numbers. Understand the pattern of square numbers in the multiplication tables. Use a multiplication grid to circle each square number. Can children spot a pattern? 8 × 8 = 64 8² = 64

	8 is a cube number.	12 is not a square number, because you cannot multiply a whole number by itself to make 12.	
Multiplying by 10, 100 and 1,000	Use place value equipment to multiply by 10, 100 and 1,000 by unitising. 4 × I = 4 ones = 4 4 × I0 = 4 tens = 40 4 × I00 = 4 hundreds = 400	Understand the effect of repeated multiplication by 10.	Understand how exchange relates to the digits when multiplying by 10, 100 and 1,000. H T O T 17 × 10 = 170 17 × 100 = 17 × 10 × 10 = 1,700 17 × 1,000 = 17 × 10 × 10 × 10 = 17,000
Multiplying by multiples of 10, 100 and 1,000	Use place value equipment to explore multiplying by unitising. 5 groups of 3 ones is 15 ones. 5 groups of 3 tens is 15 tens. So, I know that 5 groups of 3 thousands would be 15 thousands.	Use place value equipment to represent how to multiply by multiples of 10, 100 and 1,000.	Use known facts and unitising to multiply. $5 \times 4 = 20$ $5 \times 40 = 200$ $5 \times 400 = 2,000$ $5 \times 4,000 - 20,000$ $5,000 \times 4 = 20,000$
Multiplying up to 4-digit	Explore how to use partitioning to multiply efficiently.	Represent multiplications using place value equipment and add the 1s, then 10s, then 100s, then 1,000s.	Use an area model and then add the parts.

numbers by a single digit

8 × 17 = ?



00000	000000
8 × 7 = 56	

	100	60	3
5	$100 \times 5 = 500$	$60 \times 5 = 300$	3 × 5 = 15

Use a column multiplication, including any required exchanges.

Multiplying 2digit numbers by 2-digit numbers

Partition one number into 10s and 1s, then add the parts.

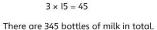
80 + 56 = 136

So, $8 \times 17 = 136$



+ 4 5

3 4 5



$$23 \times 15 = 345$$

Use an area model and add the parts.

T

000000

000000000

0000000

000000

000000

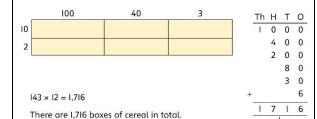
H

	20 m	8 m	Н	Т	0
			2	0	0
10 m	$20 \times 10 = 200 \text{ m}^2$	$8 \times 10 = 80 \text{ m}^2$	1	0	0
				8	0
			+	4	0
5 m	$20 \times 5 = 100 \text{ m}^2$	$8 \times 5 = 40 \text{ m}^2$	4	2	0
				Ī.	

Use column multiplication, ensuring understanding of place value at each stage.

Multiplying up to 4-digits by 2-digits

Use the area model then add the parts.



 $143 \times 12 = 1,716$

Use column multiplication, ensuring understanding of place value at each stage.

Progress to include examples that require multiple exchanges as understanding, confidence and fluency build.

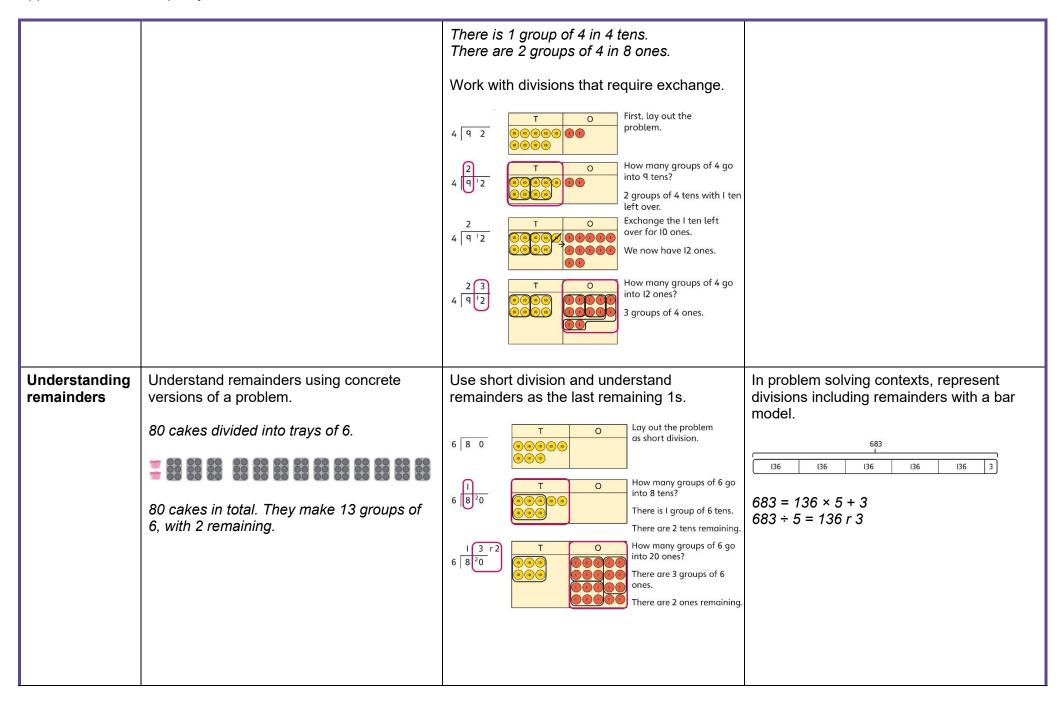
Then multiply 1,274 by 30.

Finally, find the total.

Multiplying decimals by 10, 100 and 1,000	Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths.	Represent multiplication by 10 as exchange on a place value grid. Output The Hth	Understand how this exchange is represented on a place value chart. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
Year 5 Division			
Understanding factors and prime numbers	Use equipment to explore the factors of a given number. 24 ÷ 3 = 8 24 ÷ 8 = 3 8 and 3 are factors of 24 because they divide 24 exactly. 24 ÷ 5 = 4 remainder 4. 5 is not a factor of 24 because there is a remainder.	Understand that prime numbers are numbers with exactly two factors. $13 \div 1 = 13$ $13 \div 2 = 6 r 1$ $13 \div 4 = 4 r 1$ 1 and 13 are the only factors of 13. 13 is a prime number.	Understand how to recognise prime and composite numbers. I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder. I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33. I know that 1 is not a prime number, as it has only 1 factor.
Understanding inverse operations and the link with multiplication, grouping and sharing	Use equipment to group and share and to explore the calculations that are present. I have 28 counters. I made 7 groups of 4. There are 28 in total.	Represent multiplicative relationships and explore the families of division facts.	Represent the different multiplicative relationships to solve problems requiring inverse operations.

	I have 28 in total. I shared them equally into 7 groups. There are 4 in each group. I have 28 in total. I made groups of 4. There are 7 equal groups.	60 ÷ 4 = 15 60 ÷ 15 = 4	12 ÷ 3 =
			them using inverse operations. 22 ÷ ? = 2 22 ÷ 2 = ? ? ÷ 2 = 22 ? ÷ 22 = 2
Dividing whole numbers by 10, 100 and	Use place value equipment to support unitising for division.	Use a bar model to support dividing by unitising.	Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.
1,000	4,000 ÷ 1,000	380 ÷ 10 = 38	Th H T O O O O O O O O O O O O O O O O O O
	4,000 is 4 thousands. 4 × 1,000= 4,000	10 ×	3,200 is 3 thousands and 2 hundreds. 200 ÷ 100 = 2 3,000 ÷ 100 = 30 3,200 ÷ 100 = 32
	So, 4,000 ÷ 1,000 = 4	380 is 38 tens. 38 × 10 = 380 10 × 38 = 380 So, 380 ÷ 10 = 38	So, the digits will move two places to the right.
Dividing by multiples of 10, 100 and 1,000	Use place value equipment to represent known facts and unitising.	Represent related facts with place value equipment when dividing by unitising.	Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check.
·			3,000 ÷ 5 = 600 3,000 ÷ 50 = 60 3,000 ÷ 500 = 6 5 × 600 = 3.000
			5 × 600 – 3,000

	15 ones put into groups of 3 ones. There are 5 groups. 15 ÷ 3 = 5 15 tens put into groups of 3 tens. There are 5 groups. 150 ÷ 30 = 5	180 is 18 tens. 18 tens divided into groups of 3 tens. There are 6 groups. 180 ÷ 30 = 6 1	50 × 60 = 3,000 500 × 6 = 3,000
Dividing up to four digits by a single digit using short division	Explore grouping using place value equipment. 268 ÷ 2 = ? There is 1 group of 2 hundreds. There are 3 groups of 2 tens. There are 4 groups of 2 ones. 264 ÷ 2 = 134	Use place value equipment on a place value grid alongside short division. The model uses grouping. A sharing model can also be used, although the model would need adapting. Too 4 4 8 Too 1 2 4 4 8 Too 2 4 4 8 Too 3 5 5 6 6 7 7 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	Use short division for up to 4-digit numbers divided by a single digit. $ \begin{array}{cccccccccccccccccccccccccccccccccc$



Dividing decimals by 10, 100 and 1,000	Understand division by 10 using exchange. 2 ones are 20 tenths. 20 tenths divided by 10 is 2 tenths.	Represent division using exchange on a place value grid. O	Understand the movement of digits on a place value grid. O Tth Hth Thth O 8 5 O 0 38 5 O 0 38 5 O 0 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
Understanding the relationship between fractions and division	Use sharing to explore the link between fractions and division. 1 whole shared between 3 people. Each person receives one-third.	Use a bar model and other fraction representations to show the link between fractions and division. I \div 3 = $\frac{1}{3}$	Use the link between division and fractions to calculate divisions. $5 \div 4 = \frac{5}{4} = 1\frac{1}{4}$ $11 \div 4 = \frac{11}{4} = 2\frac{3}{4}$
		Year 6	
	Concrete	Pictorial	Abstract

Year 6 Addition Comparing Represent 7-digit numbers on a place value Discuss similarities and differences Use column addition where mental methods grid, and use this to support thinking and and selecting between methods, and choose efficient are not efficient. Recognise common errors efficient mental methods. methods based on the specific calculation. with column addition. Compare written and mental methods methods TTh alongside place value representations. 32,145 + 4,302 = ?40,265 43,265 3 6 4 4 7 0000 3 5 2 2 Which method has been completed 0000000 accurately? Use bar model and number line What mistake has been made? representations to model addition in problem-solving and measure contexts. Column methods are also used for decimal additions where mental methods are not +I hour efficient +8 minutes 12:05 13:05 13:13 Represent 7-digit numbers on a place value Selecting Use a bar model to support thinking in Use place value and unitising to support grid, and use this to support thinking and addition problems. mental calculations with larger numbers. mental mental methods. methods for larger numbers 257.000 + 99.000 = ? 195.000 + 6.000 = ?M HTh TTh Th H where appropriate 195 + 5 + 1 = 201£257,000 £100,000 2.411.301 + 500.000 = ?195 thousands + 6 thousands = 201thousands

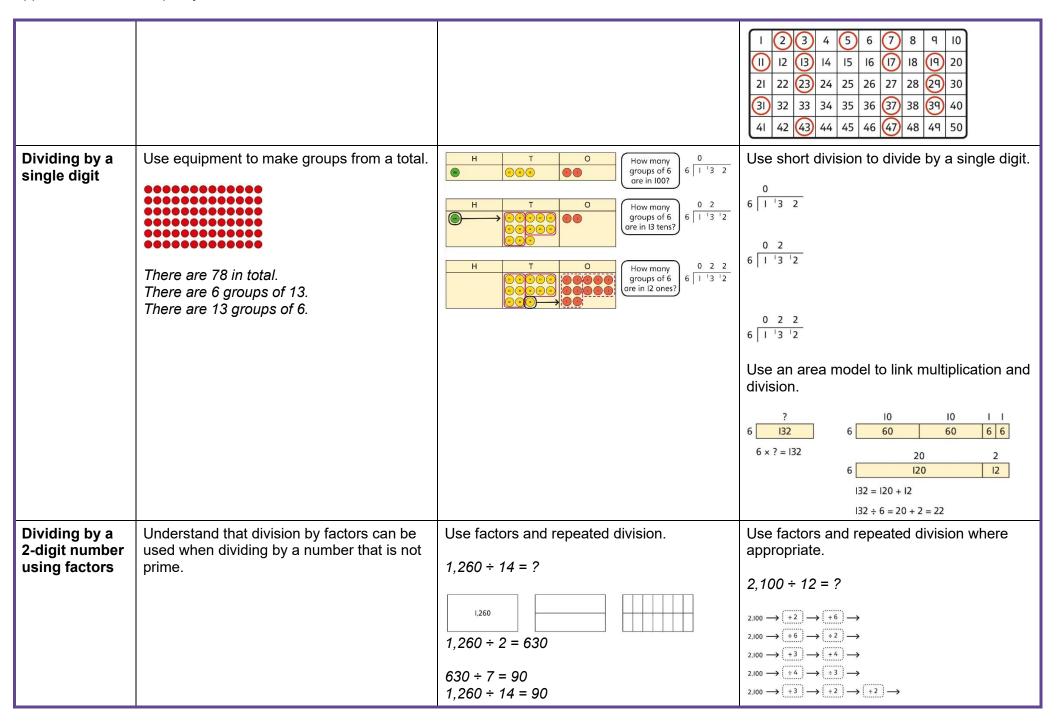
Understanding order of operations in calculations	This would be 5 more counters in the HTh place. So, the total is 2,911,301. 2,411,301 + 500,000 = 2,911,301 Use equipment to model different interpretations of a calculation with more than one operation. Explore different results. $3 \times 5 - 2 = ?$	I added 100 thousands then subtracted 1 thousand. 257 thousands + 100 thousands = 357 thousands 257,000 + 100,000 = 357,000 357,000 - 1,000 = 356,000 So, 257,000 + 99,000 = 356,000 Model calculations using a bar model to demonstrate the correct order of operations in multi-step calculations. 16 × 4	So, $195,000 + 6,000 = 201,000$ Understand the correct order of operations in calculations without brackets. Understand how brackets affect the order of operations in a calculation. $4 + 6 \times 16$ $4 + 96 = 100$ $(4 + 6) \times 16$ $10 \times 16 = 160$
Year 6 Subtraction			
Comparing and selecting efficient methods	Use counters on a place value grid to represent subtractions of larger numbers. Th H T O O O O O O O O O O O O O O O O O O	Compare subtraction methods alongside place value representations. Th H T O	Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy. The Heat Total Strategy is a selection of the column of the colum

		Th H T O 2 6 7 9 - 5 3 4 2 1 4 5 Use a bar model to represent calculations, including 'find the difference' with two bars as comparison. computer game puzzle book f12-50	Use column subtraction for decimal problems, including in the context of measure. H T O · Tth Hth 3 0 9 · 6 0 - 2 0 6 · 4 0 1 0 3 · 2 0
Subtracting mentally with larger numbers		Use a bar model to show how unitising can support mental calculations. 950,000 – 150,000 That is 950 thousands – 150 thousands 950 950 So, the difference is 800 thousands. 950,000 – 150,000 = 800,000	Subtract efficiently from powers of 10. 10,000 - 500 = ?
Year 6 Multiplication			
Multiplying up to a 4-digit number by a single digit number	Use equipment to explore multiplications. Th H T O O O O O O O O O O O O O O O O O O	Use place value equipment to compare methods. Method I 3 2 2 5 3 2 2 5 3 2 2 5 1 2 9 0 0 1 1 2	Understand area model and short multiplication. Compare and select appropriate methods for specific multiplications.

			Mathed 2
	2,345 × 4	Method 2	Method 3 3.000 200 20 5 4 12.000 800 80 20 12.000 + 800 + 80 + 20 = 12,900 Method 4 3 2 2 5 × 4 1 2 9 0 0
Multiplying up to a 4-digit number by a 2-digit number		Use an area model alongside written multiplication. Method I 1,000	Use compact column multiplication with understanding of place value at all stages. 1
Using knowledge of factors and partitions to compare methods for multiplications	Use equipment to understand square numbers and cube numbers. $5 \times 5 = 5^2 = 25$ $5 \times 5 \times 5 = 5^3 = 25 \times 5 = 125$	Compare methods visually using an area model. Understand that multiple approaches will produce the same answer if completed accurately.	Use a known fact to generate families of related facts. 170 × 1

		5,200 20 5,200 × 25 5,200 × 25	Use factors to calculate efficiently. 15×16 $= 3 \times 5 \times 2 \times 8$ $= 3 \times 8 \times 2 \times 5$ $= 24 \times 10$ $= 240$
		Represent and compare methods using a bar model.	
Multiplying by 10, 100 and 1,000	Use place value equipment to explore exchange in decimal multiplication. To the place value equipment to explore exchange in decimal multiplication. To the place value equipment to explore exchange in decimal multiplication. To the place value equipment to explore exchange in decimal multiplication. Exchange each group of ten tenths. O·3 × 10 = ? O·3 is 3 tenths. 10 × 3 tenths are 30 tenths. 30 tenths are equivalent to 3 ones.	Understand how the exchange affects decimal numbers on a place value grid. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100 and 1,000. $8 \times 100 = 800$ $8 \times 300 = 800 \times 3$ $= 2,400$ $2.5 \times 10 = 25$ $2.5 \times 20 = 2.5 \times 10 \times 2$ $= 50$
Multiplying decimals	Explore decimal multiplications using place value equipment and in the context of measures. OI O	Represent calculations on a place value grid.	Use known facts to multiply decimals. $4 \times 3 = 12$ $4 \times 0.3 = 1.2$ $4 \times 0.03 = 0.12$ $20 \times 5 = 100$ $20 \times 0.5 = 10$ $20 \times 0.05 = 1$

 $3 \times 3 = 9$ 3 groups of 4 tenths is 12 tenths. Find families of facts from a known $3 \times 0.3 = 0.9$ 4 groups of 3 tenths is 12 tenths. multiplication. Tth I know that $18 \times 4 = 72$. This can help me work out: I-3 cm I-3 cm I-3 cm 4×1 cm = 4 cm $1.8 \times 4 = ?$ $4 \times 0.3 \text{ cm} = 1.2 \text{ cm}$ $18 \times 0.4 = ?$ $4 \times 1.3 = 4 + 1.2 = 5.2$ cm Understand the link between multiplying $180 \times 0.4 = ?$ decimals and repeated addition. $18 \times 0.04 = ?$ +0.2 +0.2 +0.2 +0.2 Use a place value grid to understand the effects of multiplying decimals. Tth Hth 0 2×3 0.2×3 0 6 0.02×3 Year 6 Division **Understanding** Use equipment to explore different factors Recognise prime numbers as numbers Recognise and know primes up to 100. having exactly two factors. Understand the Understand that 2 is the only even prime, factors of a number. link with division and remainders. and that 1 is not a prime number. 0000000 $24 \div 4 = 6$ $30 \div 4 = 7 \text{ remainder } 2$ $17 \div 3 = 5 \cdot 72$ $17 \div 4 = 4 \cdot 71$ $17 \div 5 = 3 \cdot 72$ $17 \div 2 = 8 \text{ r I}$ 4 is a factor of 24 but is not a factor of 30.



Dividing by a 2-digit number using long division Use equipment to build numbers from groups.



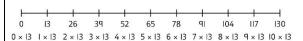
182 divided into groups of 13. There are 14 groups.

Use an area model alongside written division to model the process.

$$377 \div 13 = 29$$

Use long division where factors are not useful (for example, when dividing by a 2-digit prime number).

Write the required multiples to support the division process.



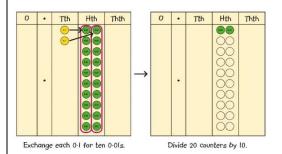
$$377 \div 13 = 29$$

A slightly different layout may be used, with the division completed above rather than at the side.

Divisions with a remainder explored in problem-solving contexts.

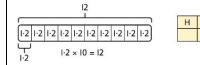
Dividing by 10, 100 and 1,000

Use place value equipment to explore division as exchange.



0·2 is 2 tenths. 2 tenths is equivalent to 20 hundredths. 20 hundredths divided by 10 is 2 hundredths. Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid.

1 • 2



Understand how to divide using division by 10, 100 and 1,000.

Use knowledge of factors to divide by multiples of 10, 100 and 1,000.

$$40 \longrightarrow \div 10 \longrightarrow \div 5 \longrightarrow ?$$

$$40 \longrightarrow \div 5 \longrightarrow \div 10 \longrightarrow ?$$

$$40 \div 5 = 8$$

 $8 \div 10 = 0.8$

So,
$$40 \div 50 = 0.8$$

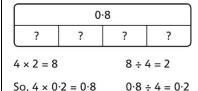
Dividing decimals

Use place value equipment to explore division of decimals.



8 tenths divided into 4 groups. 2 tenths in each group.

Use a bar model to represent divisions.



Use short division to divide decimals with up to 2 decimal places.

$$0 \cdot 5 \ 3$$
 $4 \cdot 4^{2} \cdot 4$